# Forecasting the sugarcane yields based on meteorological data through ensemble learning

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**ABSTRACT** Accurate prediction of sugarcane yields is crucial, particularly for developing countries like India, due to its economic significance and impact on farmers' livelihood. Unexpected fluctuations in production can affect farmers' income and the stability of the market, emphasizing the necessity of accurate forecasting to avoid adverse economic consequences. This research aims to enhance the precision of sugarcane yield prediction in India by developing a stacking ensemble learning model. The developed model incorporates the least absolute shrink and selection operator (LASSO), artificial neural network (ANN), and random forest (RF) as base models alongside random forest regression (RFR) and Ridge regression (RR) as meta-models and utilizes principal component analysis (PCA) and SHAPLEY values to reduce dimensions and explore feature correlations within the dataset. The data used in the study is obtained from ICRISAT and NASA databases covering 40 years (1982 to 2021) of meteorological information and sugarcane yield data across 24 districts of Uttar Pradesh, India. The model's generalizability is further improved through 5-fold cross-validation. For comparison, the vector autoregression moving average (VARMA) statistical method was also applied and it was observed that the outcome was not desirable. The findings indicate competence of stacking ensemble model over individual models like LASSO, ANN, KNN, RF, and SVR.

**INDEX TERMS** Sugarcane Forecasting, Ensemble learning, Machine learning, Agriculture, Meteorological Data.

### ABBREVIATIONS

VARMA, Vector Autoregression Moving Average; ML, Machine learning; EL, Ensemble learning; RF, Random Forest; ANNs, Artificial Neural Networks; KNN, k-nearest neighbour; RF, Random forest; LASSO, The least absolute shrink and selection operator regression; RR, Ridge regression, RFR, Random Forest Regressor; PCA, Principal Component Analysis; R<sup>2</sup>, Coefficient of determination; RMSE, Root Mean Square Error; MAE, Mean Absolute Error; MSE, Mean Squared Error; MAPE, Mean Absolute Percentage Error; GDP, Gross Domestic Product; CCF, Comprehensive Climate Factor; UP, Uttar Pradesh; ICRISAT, International Crops Research Institute for the Semi-Arid Tropics; NASA, National Aeronautics and Space Administration; CV, Cross Validation; kPa, Kilo Pascal; m/s, Meter/Second; wfv, Water Fraction by Volume.

# I. INTRODUCTION

India is one of the world's largest producers of sugarcane after Brazil [1]. Sugarcane is a crucial cash crop that plays a vital role in the country's agricultural economy. The cultivation of sugarcane serves as a dual powerhouse, boosting the national Gross Domestic Product and serving as the lifeblood for millions of farmers and industry laborers. This versatile plant produces various sugars and holds potential as a renewable energy source, capable of generating electricity, various bio-products, and biofuels. Due to its multifaceted nature, it is also known as "Wonder Cane" [2].

Accurate prediction of sugarcane yield holds significant importance in India's agricultural as well as economic sector [3]. The correlation between crop yield and market prices is deeply interconnected. Unexpected decline in production can lead to reduced surplus available for sale and diminished earnings for farmers, resulting in price hikes. Conversely, excessive production can trigger price drops, adversely affecting farmers' incomes [4]. The impact of price fluctuations of sugarcane plays a pivotal role in determining inflation rates, wages, salaries, and various economic strategies. The cost of raw materials of sugarcane for companies and their competitive positions in the market are directly impacted by production levels [5].

Various factors, from the unpredictable nature of weather patterns to developments in agricultural technology, impact the production of crops [6], [7]. Factors such as traits inherent in seeds, methods to combat pests, improved management techniques, and adjustments in the application of fertilizers play important roles in managing crop yield. Other factors that influence the yield of sugarcane include diverse land types, limited resource availability, and fluctuating weather patterns [8], [9], [10].

Scientists across the globe are focusing on methods that can predict crop yields as accurately and as consistently as possible [11], [12]. Initially, sugarcane yield forecasting focused on statistical models such as ARIMA, SARIMA, and Exponential Smoothing [13], [14]. However, as research progressed, attention shifted towards exploring more advanced techniques, including regression analysis [15], machine learning algorithms[16], and crop simulation models. Nowadays, the integration of machine learning and artificial intelligence has encouraged their extensive utilization in agriculture, especially for forecasting crop yields [17] [18]. In conventional machine learning methods. predicting agricultural output from meteorological data typically involves utilizing a single model, like linear regression or decision trees [19]. While these models can provide reasonable predictions under certain conditions, they may not fully capture the complexities and nuances present in the relationships between meteorological factors and crop yields [20], [21], [22].

In contrast, Ensemble Learning (EL) offers a more efficient solution to enhance predictive accuracy by combining the strengths of multiple models [23]. EL combines several independent models, also referred to as weak learners or base models, to generate a prediction model that is more reliable and accurate [24]. The core principle behind EL lies in the belief that the collective wisdom of several models can outperform any individual model since the errors made by individual models often offset or diminish within the ensemble [25]. By obtaining reliable predictions, farmers can proactively prepare and implement suitable strategies to tackle future challenges in agriculture [26] [27]. Table I provides the prior works in the domain of yield forecasting.

The present research aims to exploit the potential of EL in developing a robust model for forecasting sugarcane yields in India.

The developed approach integrates five distinct machine learning models, from which the top three performers are chosen as base models for stacking, and then RR and RFR are used as meta models. Additionally, feature analysis is conducted to understand the relative importance of meteorological variables in predicting sugarcane yields. Furthermore, dimensionality reduction techniques such as PCA and Shapley values have been incorporated to improve computational efficiency and streamline model performance. For improving the generativity of the model 5-fold crossvalidation technique has been used. Statistical technique VARMA has also been used for forecasting and comparing the results with EL techniques.

The rest of this paper is organized as follows: Section II describes the materials and methods. Section III discusses

the experimental results and comparison. Section IV shows the analysis and discussion. Finally, the conclusion is presented in Section V.

# II. MATERIALS AND METHODS

In this section, study area is described along with data collection process and the methodology developed for the proposed stacking EL model.

# A. STUDY AREA

Study area taken is of Uttar Pradesh (UP), situated in the northern part of India with an area of 243286 km<sup>2</sup> with coordinates 26.85°N 80.91°E. UP covers 48% of the nation's sugarcane cultivation area and contributes 50% of the total production of India, making it the leading sugarcane-producing state in India [28] offering ideal growing conditions for sugarcane like sufficient sunshine, suitable temperature, simultaneous rainfall and heat, and moderate precipitation.

Sugarcane and climatic data were collected for twenty-four districts of UP, known for their significant sugarcane production. This data covers a period between 1982 to 2021. Figure 1 shows the geographical location of the area considered in this study [29].

# **B. DATA COLLECTION**

### 1) YIELD DATA

Datasets with respect to yield were obtained from International Crops Research Institute for the Semi-Arid Tropics (ICRISAT) databases from the prominent website <u>https://www.icrisat.org//?s=sugarcane</u> [30]. A comprehensive collection of 24 district-level datasets pertaining to sugarcane production and planting areas was compiled for around 40 years, from 1982 through 2021. Equation (1) given below is used for calculating sugarcane yield:

$$Y_i = \frac{P_i}{A_i} \tag{1}$$

where  $Y_i$  is the yield of sugarcane;  $P_i$  is the district-level sugarcane production and  $A_i$  is the planted area of sugarcane at the district level. Figure 2 displays a portion of data concerning the top five sugarcane-producing districts. It includes information on area, production, and yield for each district.

# 2) METEOROLOGICAL DATA

The meteorological data sets were collected from NASA <u>https://power.larc.nasa.gov/data-access-viewer/.</u> [31]. The geographic spread of these meteorological observation stations is illustrated in Figure 2. Table II provides the meteorological variables that are considered for the present analysis.

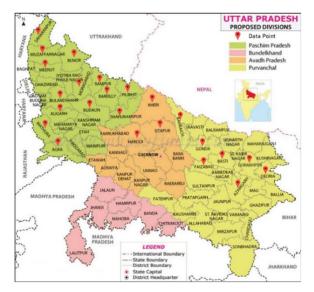


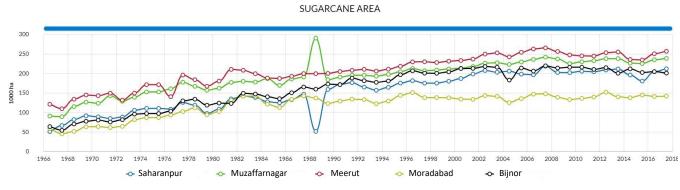
Figure 1. Geographical map of UP [29]

TABLE I
PREVIOUS WORKS DONE ON ESTIMATING THE YIELD FOR DIFFERENT CROPS

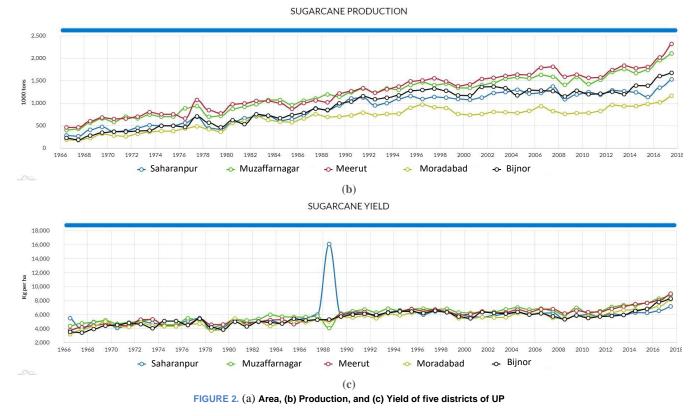
Year	Objective	WORKS DONE ON ESTIMATING THE YIE Method(s) used	Data	Study Area
2011[32]	To forecast the sugarcane	Univariate ARIMA models	Sugarcane production data from	Tamil Nadu, India
[]	area, production, and yield		1950 to 2007	
2011[33]	To forecast the sugarcane	Univariate ARIMA models	Sugarcane production data from	Uttar Pradesh and
	area, production, and		1950 to 2012	Tamil Nadu, India
	productivity			
2019[21]	EL for a cropping systems	LASSO Regression, RR, RF,	Maize Management, cultivar,	Kelley and
	simulator (APSIM) to forecast	Extreme Gradient Boosting,	and environmental factors taken	Nashua, United
2020171	the production of maize	and their ensembles	from 1983 to 2016	States of America
2020[6]	To explore the influence of historical climate fluctuations	DSSAT crop model	Five main cereal crops: barley, maize, millet, sorghum, and	Ethiopia
	on the yields of five major		wheat yield data from 1979 to	
	cereal crops		2014:	
2021[34]	To check the impact of	CCF approach determines the	Socio-economic and climate data	North and South
	climate variability on yield	sensitivity	for Rice, Maize, and Wheat from	regions of China
	variation		1981 to 2015	
2021[35]	To investigate the best	Different variants of ARIMA	Sugarcane production data from	Uttar Pradesh,
	ARIMA model for sugarcane	model	1950 to 2018	India
2021[26]	yield forecasting To forecast sugarcane yield	Statistical model using	35 years of historical weather	Uttar Pradesh,
2021[36]	using Various weighted and	regression techniques	and sugarcane yield data from	India
	un-weighted weather indices	regression teeninques	1981 to 2015	mula
2021[9]	To investigate varying trends	Regression modelling and	Wheat yield data from 1986 to	India
	in ten climate variable and	correlation analysis	2015	
	their impact on the wheat			
	yield in India			
2022[37]	To evaluate the effects of	DSSAT-CROPGRO soybean	Weather and Soybeans yield data	Northeast China
	severe climatic indices and the	model	from 1981 to 2017	
	mean climate on the actual			
	and simulated yields of			
2023[38]	soybeans To develop climate-based	ML algorithms: MLR, MLP,	Soybean yield data from 2002 to	Mato Grosso do
2023[30]	soybean yield prediction	SVM, RF, XG Boosting	2021	Sul, Brazil
	models using machine	2 ·, iu , ito Doobung		Sui, Diulli
	learning			
	0			

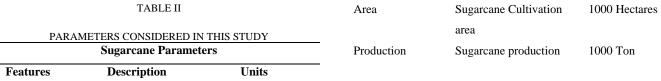


2023[39]	To estimate the crop yield using ML techniques	ML algorithms: RF, SVR, LSTM, Gradient Descent, LASSO	Yield data of Mustard Wheat, Barley, Bajra, Jowar, Onion, and Maize crops from 33 districts from 1997to 2019	Rajasthan, India
2023[24]	To develop a soybean forecasting model based on the stacking EL framework using weather parameters	KNN, RF and SVR used as the base-models and RR as meta model to establish stacking EL framework	Meteorological records along with Soybean yield data spanning a period of 34 years.	China









IEE	<b>E</b> Access
Multidisciplinary	Rapid Review Open Access Journal

Yield	Yield Production of sugarcane	
(Productivity)	per unit area	Hectare
М	eteorological Parameters	
Features	Description	Units
PS	Surface Pressure	kPa
T2M	Temperature at 2 Meters	°C
T2M_MAX	Temperature at 2 Meters	°C
	Maximum	
T2M_MIN	Temperature at 2 Meters	°C
	Minimum	
PRECTOTCORR	Precipitation Corrected	mm/day
QV2M	Specific Humidity at 2	grams of
	Meters: It is the water	water vapor
	vapor weight per unit of	per kilogram
	air.	of air (g/kg)
RH2M	Relative Humidity at 2	Percentage
	Meters measures the	(%)
	moisture in the air	
	compared to its	
	maximum capacity at a	
	given temperature.	
WS2M	Wind Speed at 2 Meters	m/s
WS2M_MAX	Wind Speed at 2 Meters	m/s
	Maximum	
WS2M_MIN	Wind Speed at 2 Meters	m/s
	Minimum	
GWETTOP	Surface Soil Wetness	wfv or m <sup>3</sup> m <sup>-3</sup>
GWETPROF	Profile Soil Moisture	wfv or m <sup>3</sup> m <sup>-3</sup>
GWETROOT	Root Zone Soil Wetness	wfv or m <sup>3</sup> m <sup>-3</sup>

### C. METHODOLOGY

In order to achieve the set research objectives, several steps were undertaken. First, the meteorological data related to sugarcane yield at the district level were obtained. Next, the records of sugarcane meteorological factors were averaged annually. PCA and SHAPLEY were used to reduce dimensionality and analyse feature correlations. After applying VARMA Statistical method, five machine learning models were employed, and the best three were selected for further analysis using MAPE, RMSE, MAE, and  $R^2$  values. Finally, a stacking model was developed, utilizing the prediction strengths of various machine learning algorithms to create an EL framework. We also incorporated a 5-fold cross-validation approach to enhance the model's robustness and generalizability. As shown in Figure 3, the research framework comprises four main components.

#### 1) DATA PROCESSING

Effective data pre-processing is fundamental to ensure the accuracy and robustness of sugarcane yield forecasting models. This study involves the processing of yield and meteorological data from 24 sugarcane-producing districts in Uttar Pradesh over a 40-year period.

The dataset consists of 15 input variables and one output variable, organized into a time series format with 24 rows and 16 columns for each year. Each variable is represented numerically. To prepare the data for analysis, a thorough examination was conducted to identify and address missing values, outliers, and inconsistencies. The processed data for Meerut district is shown in the Figure 4.

The meteorological data obtained included a broad range of features, including three related to soil properties, eleven related to wind and pressure, four related to humidity and precipitation, twelve in solar fluxes, and eight related to temperature. However, after consulting the farmers and plant protection experts, the dataset was refined to include 13 key features: three related to soil properties, four related to wind and surface, three related to humidity and precipitation, and three related to temperature. The original meteorological data was recorded on a monthly basis. To facilitate analysis, the data was aggregated to an annual level by calculating the average of the monthly values for each year. Finally, a dataset containing 13 features for each of the 24 districts, spanning a 40-year period was obtained.

2) FEATURE REDUCTION AND FEATURE IMPORTANCE PCA and SHAPLEY were incorporated in the study to optimize the dataset by reducing the dimensionality of the features. This analysis helped in identifying the correlation between meteorological factors and sugarcane yield.

# 3) DEVELOPING THE STACKING MODEL

Stacking EL model was developed by merging individual base models' unique strengths and traits to enhance the precision and robustness in forecasting sugarcane yields. Construction of the model is described in detail in the following subsections:

# a. CONSTRUCTION OF THE STACKING ENSEMBLE LEARNING MODEL

Stacking, also known as Stacked Generalization, is a combination technique that merges multiple base models through meta-models. Unlike traditional methods such as bagging and boosting that aggregate outcome from base learners, stacking constructs a multi-layered learning system by integrating diverse base learners for model fusion. [40]. The different Base and Meta-models used in this study are described in Table III.

To enhance the model's stability and generalizability, we used the 5-fold cross-validation approach. This approach divides the dataset into five equalsized folds, where the model is trained on four folds and



validated on the remaining fold. This process is repeated five times, ensuring that each fold serves as the validation set once. By averaging the performance metrics across all folds, we obtain a more reliable and unbiased estimate of the model's predictive accuracy. This approach mitigates the risk of overfitting and ensures that the model's performance is not dependent on a particular data split, thereby improving its generalizability to unseen data. For tuning the hyperparameters of the employed models, Grid Search CV is utilized to find the optimal hyperparameter settings. This technique systematically explores the hyperparameter space and selects the combination that results in the best model performance. Table IV displays the best-tuned parameters of all employed methods.

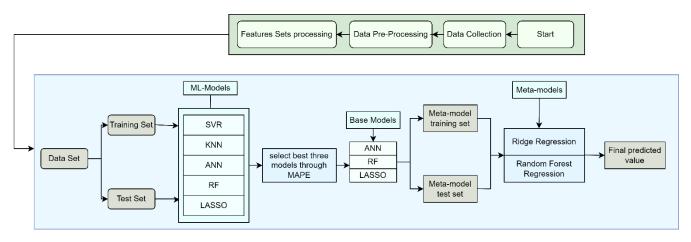


Figure 3. Sugarcane Yield Prediction Framework's Technological Roadmap

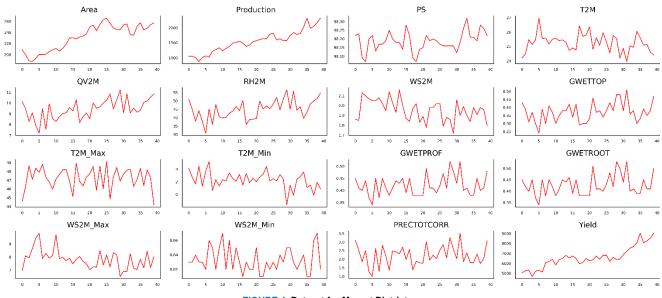


FIGURE 4. Dataset for Meerut District

ГA	BL	Æ	Π
ГA	BL	Æ	Π

METHOD & ALGORITHMS USED IN THIS STUDY							
Algorithm Definition Applicability Key Parameters							
VARMA [41]	It is a statistical method that combine vector autoregression and moving average	Dealing with interrelated time series data,	Lag order, error term, coefficient matrices	Captures complex dynamic relationship			



		multivariate time series data		in multivariate time series data
SVR[42]	It a regression-based supervised ML algorithm that finds a hyperplane to best fit data while minimizing prediction errors.	When the data has non- linear patterns and complex relationships between variables.	Kernel type, kernel parameters (e.g., gamma, degree), regularization (C), epsilon (ε)	Effective in handling non-linear relationships. It can be adapted to various kernel functions.
KNN[43]	KNN, a versatile lazy learning algorithm, handles classification and regression tasks by predicting based on the majority class or the mean of the k nearest neighbors.	When data exhibits local patterns and neighbors' behavior is relevant.	Number of neighbors (k), distance metric, weight function (uniform or distance-based), etc.	Simple and easy to understand. Non-parametric and adaptable to data changes.
RF[44]	RF, an EL algorithm, combines multiple decision trees for predictions in classification and regression tasks.	When dealing with noisy data and complex relationships between variables.	Number of trees, tree depth, minimum samples per leaf, maximum features, bootstrap samples, etc	High accuracy and robustness. Handles feature importance and variable interactions well.
LASSO[45]	LASSO, L1 regularization [46], is a linear regression technique that adds a penalty term to the linear regression objective function. It can be used for feature selection and regularization.	Dealing with high- dimensional data and multi-collinearity issues.	Regularization strength ( $\lambda$ ), alpha ( $\alpha$ )	Feature selection by shrinking some coefficients to zero. Addresses multi- collinearity effectively
ANN[47]	It is a deep-learning algorithm inspired by the human brain that comprises interconnected nodes (neurons) arranged in layers.	For capturing complex temporal dependencies and patterns in data.	Number of layers, number of neurons per layer, activation functions, learning rate, batch size, etc.	Capable of handling large and complex datasets. Suitable for capturing non-linear relationships.
RR[48]	RR, identified as L2 regularization, integrates a penalty term into the linear regression objective function to mitigate overfitting in linear regression techniques.	Dealing with multi- collinearity and overfitting issues.	Regularization strength (λ), alpha (α)	Addresses multi- collinearity by shrinking coefficients. Stabilizes parameter estimates.

### **D.** Assessment metric

The predictive method's accuracy was evaluated using four evaluation metrics:  $R^2$ , RMSE, MAE, MSE, and MAPE.  $R^2$  assesses the adequacy of the prediction model with a value closer to 1, indicating a superior fit of the regression equation. RMSE quantifies the variance between predicted and observed values, and a value closer to 0 signifies a more accurate prediction model. MAE provides insight into the actual error of the estimated values. A value closer to 0 implies a more precise model.

#### TABLE IV

VALUES OF PARAMETERS USED AFTER FINE TUNING

Methods	Parameters used
VARMA	Maxlags = 1, order = $(1,1)$
SVR	Kernel = Linear, $C=10$ , Degree = 2, Epsilon = 0.01
RF	Min-samples-leaf= 2, n-estimators = $200$
ANN	Hidden layer sizes= (100, 50), Learning rate init=0.1, Max
	iteration=1500, Optimizer= "lbfgs" stands for Limited-
	memory Broyden-Fletcher-Goldfarb-Shanno.
LASSO	Alpha = 1 (constant, controlling regularization strength)
KNN	n neighbors = 5, power parameter (p) =2, Weights =
	uniform

A lower MSE value indicates that the predicted values are closer to the actual values, signifying a more accurate model. MAPE calculates the average relative error between predicted and measured values, directly revealing the variance between predicted and actual results. A value closer to 0% indicates higher accuracy.

$$R^{2} = 1 - \frac{\sum_{i=1}^{n} (y_{i} - \hat{y}_{i})^{2}}{\sum_{i=1}^{n} (y_{i} - \bar{y}_{i})^{2}}$$
(6)

$$RMSE = \sqrt{\frac{\sum_{i=1}^{n} (y_i - \hat{y}_i)^2}{n}}$$
(7)

$$MAE = \frac{1}{n} \sum_{i=1}^{n} |y_i - \hat{y}_i| \tag{8}$$

$$MSE = \frac{1}{n} \sum_{i=1}^{n} (y_i - \hat{y}_i)^2$$
(9)

$$MAPE = \frac{1}{n} \sum_{i=1}^{n} \left| \frac{y_i - \hat{y}_i}{y_i} \right| * 100\%$$
(10)

### E. SYSTEM CONFIGURATION

The experiments were executed on Spyder 4.1.5 Integrated Development Environment (IDE) with Python 3.8 through an Anaconda distribution on an Intel Xeon W-1290P CPU @ 3.70GHz dual-processor system with 64 GB RAM, an Nvidia Quadro P1000 GPU, and a 64-bit Windows 11 Pro Operating System. All algorithms were implemented using Python, employing libraries such as Numpy, Pandas, Matplotlib, Sklearn, Seaborn, and Shap.

### III. RESULTS

# A. VARIABLE SCREENING AND DIMENSIONAL PROCESSING

This study chose a feature set comprising 15 variables and one target variable, encompassing 13 annual meteorological indicators. The results for Meerut district are being presented herein. The feature correlation matrix provides an extensive overview of the of the interrelationships among all variables considered in the analysis. It allows us to assess the strength and direction of correlations between each pair of variables, helping to identify patterns and associations within

Figure 5 displays the correlation matrix of 15 features, particularly emphasizing the variable area. From the figure, we observe that among the 15 features, 9 exhibit positive correlations, while 5 are negatively correlated with area. Production is highly correlated with area, while T2M\_max is observed to have minimal impact.

In order to address potential issues of duplicated information and limited generalizability in the feature set, PCA [49] is employed. PCA allows the transformation of a set of correlated variables into a set of uncorrelated variables while retaining the essential information from the original feature set.

PCA aims to capture the maximum information in the first principal component, the maximum remaining information in the second component, and so on, as depicted in the Scree plot figure 6. The Elbow Point in the Scree Plot is where the cumulative explained variance levels off or plateaus. It indicates that additional principal components contribute less and less to the overall variance explained. The Elbow Point occurs at PC 8 in this figure, suggesting that the first eight principal components are crucial in capturing most of the dataset's variability.

In the context of feature importance, the Shapley value assesses the contribution of each feature to the prediction by considering all possible permutations of features [50]. Figure 7(a) indicates that PS is the most important feature, followed by Qv2m, among all 15 features that are correlated to the yield.

The bar chart in figure 7(b) represents the Shapley values in descending order of all features, where higher values indicate greater importance and lower values indicate lesser importance of the feature in predicting the output variable yield.

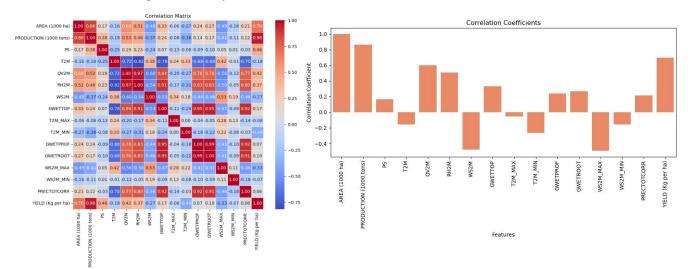
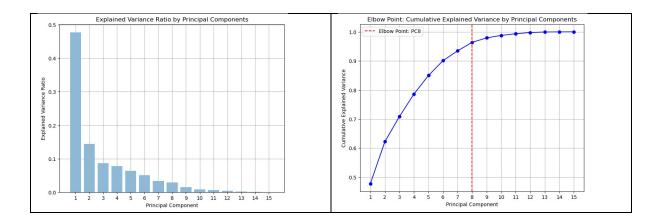
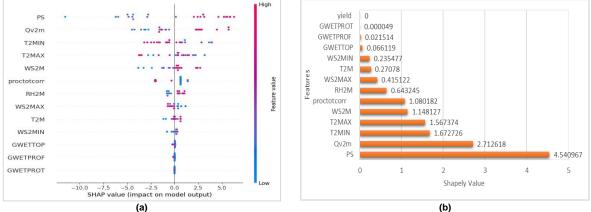


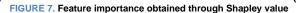
FIGURE 5. Feature Correlation matrix











### B. Base Model Selection

In the initial phase, five machine learning models (RF, ANN, KNN, SVR, and LASSO) were utilized to forecast sugarcane yield. To ensure robustness, we partitioned our dataset with 80% for training and the remaining 20% for testing purposes. Here, the results for Meerut district are shown, offering valuable insights into model performance by comparing predicted yields with actual values on the test dataset. Among the models, SVR and KNN exhibited deviations from the actual values, indicating lower accuracy. In contrast, the RF, ANN, and LASSO models demonstrated closer alignment with actual values, suggesting superior performance. Moreover, we conducted an assessment of feature importance by generating column plots for each machine learning method, shown in figure 8. This facilitated the identification of the most influential features in sugarcane yield prediction for each respective model, contributing to a deeper understanding of the predictive dynamics involved.

After the analysis, we computed the evaluation metrics for all five ML methods on the test dataset, which were used

to forecast the sugarcane yield. The results are summarized in Table V.

	TABLE V EVALUATION METRICS							
Methods	MAE	MSE	RMSE	MAPE	$R^2$			
VARMA	778.62	768545.25	876.66	8.87%	0.28			
SVR	429.31	308126.45	555.09	6.48%	0.50			
KNN	405.488	204871.46	483.47	6.42%	0.665			
RF	125.65	24864.71	157.68	1.92%	0.96			
ANN	290.25	135923.74	368.68	4.38%	0.78			
LASSO	93.91	9916.37	99.58	1.47%	0.98			

The superior performance of LASSO in comparison to other models is clearly visible through Table V for every evaluation metrics taken in this study and was it was therefore selected as the base model. Conversely, VARMA, SVR and KNN models exhibited notable underperformance, leading to their exclusion as base models for the stacking ensemble framework. RF and ANN did not perform as efficiently as LASSO but were around 50% better than SVR and KNN and were hence taken as base models along with LASSO.





FIGURE 8. Prediction of yield over time through ML Models

# C. Yield forecast

Within the stacking EL framework, RR and RFR are utilized as meta-models. Figure 9 illustrates the stacking model's performance compared to individual single models. The ensemble models utilizing the stacking EL approach showed closer alignment with actual yield values, indicating superior performance and predictive accuracy in contrast to single models. A significant improvement in closeness to actual yield values was observed when RFR was utilized as the meta-model in the stacking framework, as opposed to RR.

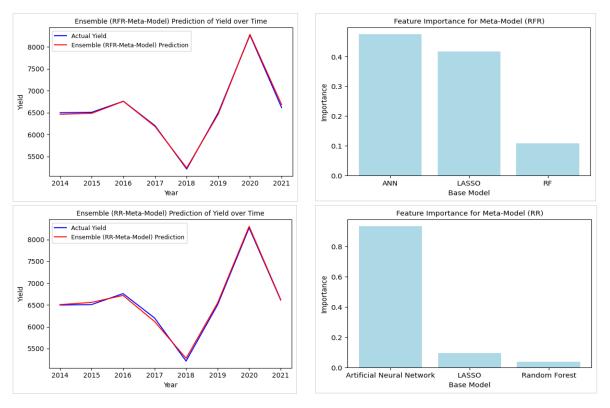


FIGURE 9. Prediction of yield over time through meta-models as RFR & RR

Table VI provides a comprehensive comparison of evaluation metrics between the stacking model and three base models. The stacking model always outperformed the individual single models. Stacking done through RFR meta-model performed better in comparison to stacking done through RR as meta model in terms of lower MAPE (0.43%), MAE (27.837), MSE (1106.698), RMSE (33.267) and  $R^2$  (0.998).

TABLE VI					
VALUATION METDICS	INCLU	IDING	STACK	INC	

EVALUATION METRICS, INCLUDING STACKING						
Index	ANN	RF	LASSO	Stacking	Stacking	
				(RR)	(RFR)	
MAE	290.25	125.65	93.91	42.006	27.837	
MSE	135923	24864.71	9916.37	2281.71	1106.698	
RMSE	368.67	157.68	99.58	47.767	33.267	
MAPE	4.38%	1.92%	1.47%	0.67%	0.43%	
$R^2$	0.778	0.959	0.98	0.996	0.998	

Figure 10 shows the results of yield forecasting using the stacking EL model, with RFR utilized as the meta-model, for the next ten years across five districts: Meerut, Moradabad, Muzaffarnagar, Bijnor, and Saharanpur. The dotted line represents the actual yield, while the asterisk line indicates

the forecasted yield for future years. The graph illustrates an upward trajectory in yield over the forthcoming years.

### **IV.** Discussion

This study addresses the need for improved sugarcane yield forecasting by utilizing meteorological data and introducing a stacking EL approach to overcome the limitations of traditional forecasting methods.

The model is designed to enhance predictive accuracy and flexibility, incorporating Principal Component Analysis (PCA) and SHAPLEY values for a better understanding of feature correlations. Accurate yield prediction is crucial for effective agricultural management, providing stakeholders with critical insights to support sustainable practices, optimize resource use, and stabilize the agricultural economy.

Previous studies on sugarcane yield forecasting have utilized simpler statistical models such as multiple linear regression and simple regression, and ARIMA, mainly considering the environmental variables such as Tmax, Tmin, Rainfall and humidity [51]. While these studies covered several years of data, they were unable to capture complex relationships between various meteorological



factors. More recent work has used various ML algorithms such as RF, SVR, and ANN, while these methods improved the accuracy of prediction but did not employ ensemble approaches, limiting the full potential of combining model strengths.

The present study improves on previous work by using 13 meteorological variables related to soil, wind, humidity, and temperature, along with area, production and yield data of sugarcane. We also applied VARMA method for multivariate time series forecasting of sugarcane yield, but the results were not satisfactory. To improve the accuracy, we implemented a stacking EL approach, which provides stronger generalization and better captures complex relationships. This method significantly enhanced the accuracy and reliability of sugarcane yield prediction, outperforming traditional models in both precision and scalability. Table VII provides a comprehensive comparison of last five years of the research in the field of sugarcane yield forecasting in India, highlights the differences in methodologies and meteorological factors used in our study and the existing body of work.

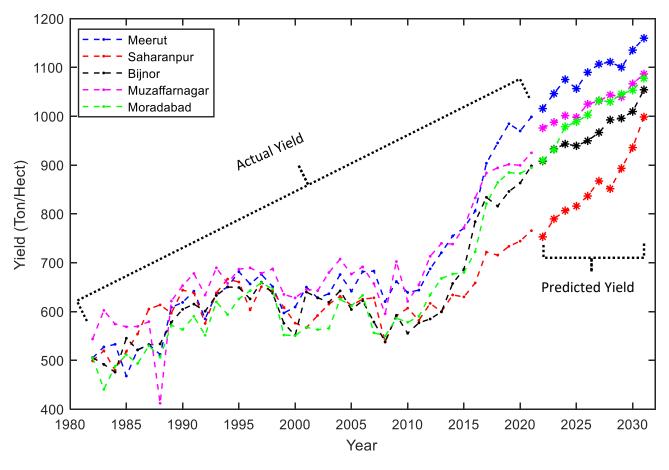


FIGURE 10. Predicted yield when meta-model as RFR

TABLE VII PREVIOUS WORK IN SUGARCANE FORECASTING



Year	No of Meteorological Parameters					Methods				Stu	Study Area	
	Temperatur e	Humidit y	Wind/ Pressur e	Soil Propertie s	Tota l	Statistical	ML	Advance d	- Data	No. of Region s	State	
2020 [52]	×	×	×	×	×	ARIMA	×	×	50 years (1967- 2016)	2	Haryana	
2021 [53]	x	x	x	x	×	ARIMA	×	×	69 years (1950- 2018)	6	Andhra Pradesh, Uttar Pradesh, Karnataka, Tamil Nadu, Maharashtr a	
2021 [54]	2	3	×	×	4	Regression Techniques	×	×	35 years (1981- 2015)	1	Uttar Pradesh	
2022 [55]	2	1	×	×	3	ARIMA, ARIMAX	×	×	40 years (1979- 2018)	3	Haryana	
2023 [56]	2	4	×	×	6	Discriminan t Function Analysis	×	×	57 years (1960- 2016)	1	Tamil Nadu	
2024 [57]	2	3	×	×	5	×	RF, SVM, SMLR, ANN	×	24 years (1997- 2020)	10	Karnataka	
Presen t Study	3	3	4	3	13	VARMA	SVR, ANN, KNN, RF, LASS O	Stacking Ensemble Learning	40 years (1982- 20021 )	24	Uttar Pradesh	

The findings of our study are significant for precise sugarcane yield predictions, particularly with ongoing impacts of climate changes on farming. By using the developed model in real world agriculture, farmers can get valuable insights about future yields considering weather conditions. With this information, farmers and decisionmakers may make better plans for maximizing their crops yield, including when to harvest, when to apply fertilizer and irrigation, and which seeds to use in response to changing weather patterns. Agribusinesses can also benefit from these predictions by optimizing their supply chains, emphasizing more efficient operations, cutting waste, and minimizing losses after harvest.

Given sugarcane's pivotal role in India's economy and the livelihoods of millions of farmers and laborers, accurate forecasting is essential for ensuring food security, stabilizing markets, and guiding policy decisions. Considering the significance of sugarcane to the Indian economy and the livelihoods of millions of people, reliable forecasting is essential for maintaining food security, stabilizing market prices, and assisting policymakers in formulating measures that better assist the agriculture sector.

# V. Conclusion

Accurate prediction of sugarcane yield is crucial for effective agricultural management and early warning systems. We utilized VARMA method to forecast the sugarcane yield by incorporating this multivariate dataset but the results were not satisfactory. So, we developed a stacking EL model. The model developed for this study comprised ANN, RF, and LASSO as base models and RFR as the meta-model and PCA aids in reducing dimensionality while preserving essential information, while SHAPLEY values offer insights into feature importance. These techniques not only enhance the predictive capability of the model but also provide interpretability. Numerical results and graphs demonstrated the efficiency of the model in terms of forecasting within primary sugarcane cultivation regions. Our approach provides a robust, data-driven framework that can be expanded to other crops and regions, contributing to more efficient and sustainable agricultural practices. Some concluding remarks that can be drawn from the current study are:

- i. In comparison to utilizing VARMA and machine learning techniques LASSO, ANN, KNN, RF, and SVR in a standalone manner, the stacking model is better for all evaluation indicators, such as MAE, MSE, RMSE, MAPE, and  $R^2$
- ii. Utilizing the strengths of its base models, the stacking model notably enhances forecast accuracy, predicting the meteorological yield of sugarcane.
- iii. The forecasting system developed in the study can help the farmers in planning cultivation strategies more effectively. It can also help the retailers n optimizing the supply chains, and policymakers to make informed decisions for resource allocation and agricultural sustainability.

Future research directions could explore refining the stacking EL approach by incorporating additional machine learning techniques or exploring alternative meta-models and uses of hybrid models that combine convolution layers to extract spatial features with recurrent layers. Also, one could explore the integration of real-time data sources, such as satellite imagery and IoT-based sensors, which could further enhance the model's responsiveness to changing environmental conditions. Additionally, expanding the model's application to different crops or geographic areas could provide valuable insights and contribute to a broader understanding of agricultural forecasting. Incorporating socio-economic factors-such as

market trends, labor availability, and policy changes—into the forecasting model could provide a more holistic view of the factors influencing crop yields.

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